Patterns of protein interactions are organized around complex heterogeneous networks. Their architecture has been suggested to be of relevance in understanding the interactome and its functional organization, which pervades cellular robustness. Transcription factors are particularly relevant in this context, given their central role in gene regulation. Here we present the first topological study of the human protein–protein interacting transcription factor network built using the TRANSFAC database. We show that the network exhibits scale-free and small-world properties with a hierarchical and modular structure, which is built around a small number of key proteins. Most of these proteins are associated with proliferative diseases and are typically not linked to each other, thus reducing the propagation of failures through compartmentalization. Network modularity is consistent with common structural and functional features and the features are generated by two distinct evolutionary strategies: amplification and shuffling of interacting domains through tinkering and acquisition of specific interacting regions. The function of the regulatory complexes may have played an active role in choosing one of them.

Abbreviations
ER, Erdős-Rényi; HTFN, human transcription factor network; SF, scale free; SW, small world; TF, transcription factor.

Keywords
human; molecular evolution; protein interaction; tinkering; transcription factor network

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allow the formation of supramolecular activator or inhibitory complexes, depending on their components and possible combinations.

Transcription factors (TFs) are an essential subset of interacting proteins responsible for the control of gene expression. They interact with DNA regions and tend to form transcriptional regulatory complexes. Thus, the final effect of one of these complexes is determined by its TF composition.

The number of TFs varies among organisms, although it appears to be linked to the organism’s complexity. Around 200–300 TFs are predicted for Escherichia coli [18] and Saccharomyces [19,20]. By contrast, comparative analysis in multicellular organisms shows that the predicted number of TFs reaches 600–820 in C. elegans and D. melanogaster [20,21], and 1500–1800 in Arabidopsis (1200 cloned sequences) [20–22]. For humans, around 1500 TFs have been documented [21] and it is estimated that there are 2000–3000 [21,23]. Such an increase in the number of TFs is associated with higher control of gene regulation [24]. Interestingly, such an increase is based on the use of the same structural types of proteins. Human transcription factors are predominantly Zn fingers, followed by homeobox and basic helix–loop–helix [21]. Phylogenetic studies have shown that the amplification and shuffling of protein domains determine the growth of certain transcription factor families [25–28]. Here, a domain can be defined as a protein substructure that can fold independently into a compact structure. Different domains of a protein are often associated with different functions [29,30].

When dealing with TF networks, several relevant questions arise. How are these factors distributed and related through the network structure? How important has the protein domain universe been in shaping the network? Analysis of global patterns of network organization is required to answer these questions.

To this end, we explored, for the first time, the human transcription factor network (HTFN) obtained from the protein–protein interaction information available in the TRANSFAC database [31], using novel tools of network analysis. We show that this approximation allows us to propose evolutionary considerations concerning the mechanisms shaping network architecture.

**Results and Discussion**

**Topological analysis**

Data compilation from the TRANSFAC transcription factor database provided 1370 human entries. After filtering according to criteria given in Experimental Procedures, a graph of \( N = 230 \) interacting human TFs was obtained (Fig. 1). This can be understood as the architecture of the regulatory backbone. It provides a topological view of the interaction patterns among the elements responsible for gene expression. This corresponds to the protein hardware that carries out genomic instructions. The remaining TFs contained in the database did not form subgraphs and appeared isolated. The relatively small size of the connected graph compared with all the entries in the database might be due, at least in part, to the current degree of knowledge of this transcriptional regulatory network, with only sparse data for many of its components. Although a number of possible sources of bias are present, it is worth noting that the topological pattern of organization reported from different sources of protein–protein interactions seems consistent [32].

Topological analysis of HTFN is summarized in Table 1 showing that HTFN is a sparse, small-world graph. The degree distribution (Fig. 2A) and clustering (Fig. 2B) show a heterogeneous, skewed shape reminding us of a power–law behaviour, indicating that most TFs are linked to only a few others, whereas a handful of them have many connections. The average betweenness centrality \( (b) \) shows well-defined power–law
scaling (Fig. 2C). Also, the network displays well-defined correlations among proteins depending on their degree. As with other complex networks, we found that the HTFN is disassortative: high-degree proteins attach to low-degree ones [33]. This is an important property as it is connected with the presence of modular organization (see below). Because hubs are linked to many other elements but tend not to link themselves, disassortativeness allows large parts of the network to be separated and thus partially isolated from different sources of perturbation.

Figure 3A,B shows the obtained correlation profiles. They are similar to that previously obtained for a protein interaction network of yeast proteome [34]. As shown in Fig. 3A, highly connected nodes associated with poorly connected ones are more abundant than predicted by a null model. By contrast, links between highly connected nodes tend to be under-represented, indicating a reduced likelihood of direct links between hubs. SF networks exhibit a high degree of error tolerance, yet they are vulnerable to attacks against hubs [35]. It seems that this has been attenuated in biomolecular networks by avoiding direct links between hubs [34]. This type of pattern is a sign of modularity: groups of proteins can be identified as differentiated parts of the web, allowing for functional diversity. Modularity can be properly detected and measured using the so-called topological overlap matrix [36]. Figure 3C shows the topological overlap matrix for HTFN. The array shows a nested, hierarchical structure with small modules as dark boxes across the diagonal, which have a large overlap. However, there are some weak connections between modules, as shown by the tiny lines in the topological overlap matrix. The algorithm weights the (topological) association of any node to the others, and it is possible to build a dendrogram of relations where we can see also a hierarchy, because modules are not related at the same level as would be expected in a pure modular network [2].

It is noteworthy that the presence of a high level of self-interaction is a prominent feature of this TF web, distinguishing it from other real networks. Indeed, 17.8% of proteins have self-interactions. Here
self-interaction is understood as the interaction between proteins of the same type, i.e. homo-oligomerization, regardless of the number of monomers involved. To evaluate their importance, we compared correlation profiles with and without self-interactions (Fig. 3A and B, respectively). Changes in the whole profile are evident, suggesting that nodes with self-interactions are distributed along the whole range of degree values. It is particularly remarkable that the intense signal around degree values of 2–3 in the profile with self-interactions (Fig. 3A) is attenuated in the corresponding profile following their deletion (Fig. 3B). Such a striking difference can be explained by an overabundance of proteins able to form homo-oligomers and to establish connections with one or two more proteins. This can be related to the small but highly integrated modules observed in the topological overlap matrix (Fig. 3C). A simple explanation for these observations can be given based on biological constrains derived from the evolution of TFs, and is discussed below.

**Functional, evolutionary and topological constrains**

**Biological function of topological relevant elements**

In order to clarify the relation between biological function and topology of HTFN, we identified in the network those factors that have the highest number of interactions (so-called hubs). In a biological context, hubs can have important roles. In metabolic networks, essential metabolites such as pyruvate and coenzyme A have been identified as hubs [36]. In relation to TFs, it has been suggested that p53 is a hub integrating regulatory interactions involving cell cycle, cell differentiation, DNA repair, senescence or angiogenesis [37]. Perhaps not surprisingly, this gene is considered a so-called Achilles’ heel of cancer [38]. Table 2 summarizes the most highly connected factors in HTFN and their related diseases. They are also highlighted in the HTFN graph (Fig. 1). It should be stressed that TATA binding protein (TBP) has the highest degree. TBP is considered a key factor for transcription initiation [39]. Its essentiality is highlighted by the fact that an aberrant version of TBP causes spinocerebellar ataxia [40] and the lack of TBP by homologous recombination leads to growth arrest and apoptosis at the embryonic blastocyst stage [41]. Other hubs, such as p53 (the second in degree) and retinoblastoma protein (pRB) are tumour suppressor proteins. Most of these highly connected factors are related to cancer.

We have seen that highly connected nodes have essential biological roles. However, because regulation can occur at different levels, such as target specificity...
or via control of TF expression, less connected factors may also be relevant to cell survival.

Functional and structural patterns from topology

In order to reveal the mechanisms that shape the structure of HTFN, we studied its topological modularity in relation to the function and structure of TFs from available information. From a structural point of view, the overabundance of self-interactions is associated with a majority group of 55% of basic helix-loop-helix (bHLH) and leucine zippers (bZip), 17.5% of Zn fingers and 22.5% corresponding to a more heterogeneous group, the ‘beta-scaffold factor with minor groove contact’ (according to the TRANSFAC classification) superclass, which includes Rel homology regions, MADS factors and others.

Such structures can be understood as protein domains, which can be found alone or combined to give rise to TFs. These domains are responsible for relevant properties, such as TF–DNA or TF–TF binding. In this context, self-interactions can be explained by the presence of domains with the ability to bind between them as is the case of bHLH and bZip. They follow a general mechanism to interact with DNA based on protein dimerization [42]. Zn finger domains are common in TFs, allowing them to bind DNA, but not to interact with other protein regions [42]. This group of self-interacting Zn finger proteins is a subset of the nuclear receptor superfamily (steroid, retinoid and thyroid, as well as some orphan receptors) [26,43]. They obey a general mechanism in which Zn finger TFs have to form dimers in order to recognize tandem sequences in DNA [42]. In fact, regulation at the level of formation of transcriptional regulatory complexes is linked to a homo/heterodimerization of TFs containing these self-interacting domains. Attending to this simple rule of domain self-interaction, relative levels of these proteins could determine the final composition of a complex, by varying their function and affinity to DNA. This is the case of the bHLH–bZip proto-oncogen c-myc [44], or the Zn finger retinoid X receptor RXR [45].

From a topological viewpoint, connections by self-interacting domains would imply high clustering and modularity, because all these proteins share the same rules and they have the potential to give a highly interconnected subgraph (i.e. a module). According to this, the high clustering of HTFN (see Fig. 1) could be explained as a by-product of the overabundance of self-interacting domains.

We wondered whether the HTFN modular architecture (Fig. 3C) might include both functionality and structural similarity. In order to simplify the study of modularity, we traced an arbitrary line identifying seven putative protein groups (dashed line in Fig. 3C). Nodes of each group were identified by different colours in the HTFN graph (Fig. 4A) where we visualize the modules defined by the topological overlap algorithm. We note that a consequence of the hierarchical component of HTFN is that not all factors in each group have the same level of relation. Unlike a simple modular network, the combination of hierarchy and modularity cannot give homogeneous groups.

Figure 4B shows the HTFN core graph, highlighting its modularity, the under-representation of connections between hubs and the overabundance of highly connected nodes linked to poorly connected ones (both observed in the correlation profile). The central role of the hubs in topological groups defined in Fig. 3A should be stressed, such hubs are those described in Table 2, with the exception of E12 (with k = 11), which is involved in lymphocyte development [46].

An analysis of the topological modules of the Fig. 3 (labelled A–G) shows that they include structural and/or functional features. Table 3 summarizes the main structural and functional features of these groups. In agreement with the structural homogeneity

<table>
<thead>
<tr>
<th>TF</th>
<th>Description</th>
<th>Associate disease</th>
<th>Associate disease</th>
<th>k</th>
<th>b x 10^3</th>
</tr>
</thead>
<tbody>
<tr>
<td>TBP</td>
<td>Basal transcription machinery initiator</td>
<td>Spinocebelar ataxia [40]</td>
<td>Spinocebelar ataxia [40]</td>
<td>27</td>
<td>17.3</td>
</tr>
<tr>
<td>TBP</td>
<td>Basal transcription machinery initiator</td>
<td>Spinocebelar ataxia [40]</td>
<td>Spinocebelar ataxia [40]</td>
<td>27</td>
<td>17.3</td>
</tr>
<tr>
<td>p53</td>
<td>Tumor suppressor protein</td>
<td>Proliferative disease [68]</td>
<td>Proliferative disease [68]</td>
<td>23</td>
<td>18.5</td>
</tr>
<tr>
<td>p53</td>
<td>Tumor suppressor protein</td>
<td>Proliferative disease [68]</td>
<td>Proliferative disease [68]</td>
<td>23</td>
<td>18.5</td>
</tr>
<tr>
<td>P300</td>
<td>Coactivator. Histone acetyltransferase</td>
<td>May play a role in epithelial cancer [69]</td>
<td>May play a role in epithelial cancer [69]</td>
<td>18</td>
<td>20.2</td>
</tr>
<tr>
<td>P300</td>
<td>Coactivator. Histone acetyltransferase</td>
<td>May play a role in epithelial cancer [69]</td>
<td>May play a role in epithelial cancer [69]</td>
<td>18</td>
<td>20.2</td>
</tr>
<tr>
<td>RXR-α</td>
<td>Retinoid X-α receptor</td>
<td>Hepatocellular carcinoma [70]</td>
<td>Hepatocellular carcinoma [70]</td>
<td>18</td>
<td>8</td>
</tr>
<tr>
<td>RXR-α</td>
<td>Retinoid X-α receptor</td>
<td>Hepatocellular carcinoma [70]</td>
<td>Hepatocellular carcinoma [70]</td>
<td>18</td>
<td>8</td>
</tr>
<tr>
<td>pRB</td>
<td>Retinoblastoma suppressor protein.</td>
<td>Proliferative disease Bladder cancer.</td>
<td>Proliferative disease Bladder cancer.</td>
<td>15</td>
<td>27.1</td>
</tr>
<tr>
<td>pRB</td>
<td>Retinoblastoma suppressor protein.</td>
<td>Proliferative disease Bladder cancer.</td>
<td>Proliferative disease Bladder cancer.</td>
<td>15</td>
<td>27.1</td>
</tr>
<tr>
<td>RelA</td>
<td>NF-κB pathway</td>
<td>Hepatocyte apoptosis and foetal death [72]</td>
<td>Hepatocyte apoptosis and foetal death [72]</td>
<td>14</td>
<td>6.6</td>
</tr>
<tr>
<td>RelA</td>
<td>NF-κB pathway</td>
<td>Hepatocyte apoptosis and foetal death [72]</td>
<td>Hepatocyte apoptosis and foetal death [72]</td>
<td>14</td>
<td>6.6</td>
</tr>
<tr>
<td>c-jun</td>
<td>AP-1 complex (activator). Proto-oncogen</td>
<td>Proliferative disease [73]</td>
<td>Proliferative disease [73]</td>
<td>14</td>
<td>4.1</td>
</tr>
<tr>
<td>c-jun</td>
<td>AP-1 complex (activator). Proto-oncogen</td>
<td>Proliferative disease [73]</td>
<td>Proliferative disease [73]</td>
<td>14</td>
<td>4.1</td>
</tr>
<tr>
<td>c-myc</td>
<td>Activator. Proto-oncogen</td>
<td>Proliferative disease [74]</td>
<td>Proliferative disease [74]</td>
<td>13</td>
<td>10.5</td>
</tr>
<tr>
<td>c-myc</td>
<td>Activator. Proto-oncogen</td>
<td>Proliferative disease [74]</td>
<td>Proliferative disease [74]</td>
<td>13</td>
<td>10.5</td>
</tr>
<tr>
<td>c-fos</td>
<td>AP-1 complex (activator). Proto-oncogen</td>
<td>Proliferative disease [75]</td>
<td>Proliferative disease [75]</td>
<td>12</td>
<td>2</td>
</tr>
<tr>
<td>c-fos</td>
<td>AP-1 complex (activator). Proto-oncogen</td>
<td>Proliferative disease [75]</td>
<td>Proliferative disease [75]</td>
<td>12</td>
<td>2</td>
</tr>
</tbody>
</table>
of TFs, the most representative groups are A and B and F followed by group C with two main structural domains. By contrast, the groups with the highest structural heterogeneity are D, E and G (see details in Table 3).

In relation to functionality, group B exhibits a clear homogeneity because is made of the so-called c-myc/mad/max network (bHLH–bzip domains) [47] and other related factors such as rox [48], mxi [47], miz-1 [49] TTRAP, GNC5, bin-1 [50]. Group F contains 90% of the members of the nuclear receptor hormone superfamily of the HTFN (they also are Zn finger proteins) [26]. In these groups, functionality and structural homogeneity appear to be related. Group E is made of TATA-binding protein-associated proteins, representing the conserved basal transcription machineries for different promoter types from yeast to humans [51]. Other factors in group E are not part of these basal machineries but are closely related to the TBP. Thus, we can say that group E has clear functionality in transcription initiation. Unlike other groups, its components do not show structural similarities, with the exception of some TAFII and NC2 and NF-Y factors that have histone fold motifs [52]. Group G is a small subset that contains all the SMAD proteins of the HTFN and APC and β-catenin-related factors.

Groups C and D involve smaller functional sets. Group C contains the Rel family and CRE binding factors involved in the NFκB pathway and other functional related factors, such as p300 and CBP. Group D contain factors related to cell cycle and DNA repair-related factors (p53 and its direct interactors, and BCRA). It is noteworthy that it contains the structural and functional E2F/pRB pathway, which is made of a group of fork-head transcription factors (E2F and DP factors) and retinoblastoma proteins (pRB, p107 and p130) [53]. Moreover, it also appears related to histone deacetylases. This topological homogeneous module involves the regulatory mechanism by means of which pRB interacts with E2F proteins and is involved in the recruitment of histone deacetylases in order to carry out the transcriptional repression [54]. Factors involved in DNA repair, such as p53 (and its direct interactors) and BCRA, appear also close in the dendogram.

**Evolutionary implications of the HTFN topology**

Phylogenetic studies about the main protein structure types in HTFN such as the Zn finger nuclear receptor and bHLH domains suggest that they were expanded by a diversification process derived from common ancestral genes via duplication and exon shuffling [28,55]. They are believed to have expanded together with the appearance of multicellularity, becoming required for the new functional regulations derived
It has been suggested that Zn finger nuclear receptors (group E) are derived from a common ancestral gene [26]. In the case of bHLH TFs, it is remarkable that topological groups A and B are made of TFs belonging to the phylogenetic E-box types A and B [55], respectively. It suggests that phylogeny can also be retained by the topology. They made a topological group due to the self-interacting property of the bHLH domains. Therefore, this seems to be a topological constrain derived from the evolution of this family.

Evolution based on domain reusing might explain the abundance of certain protein domains and is a way of easily increasing the number of TFs, as appears to have occurred through evolution. Functionality can be linked to structure, as is the case of DNA-binding and Zn finger domains, or the fork-head DNA-binding domains in the E2F/pRB pathway [56]. Another example is the enzymatic activity of histone deacetylases, contained in this network.

<table>
<thead>
<tr>
<th>Group</th>
<th>No. of TF</th>
<th>Structural features</th>
<th>Functional features</th>
<th>TFs</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>22</td>
<td>77% bHLH domains.</td>
<td>Muscle and neural tissue specific, sex determination. Includes E proteins family related to lymphocyte differentiation [46,55]. Includes E-box type A TF.</td>
<td>Ly1, Lmo2, Lmo1, MEF-2, MEF-2DAB, ITF-1, E12, E47, ITF-2, HEB, Id2, Tal-1, MyoD, Myf-4, Myf-5, Myf-6, Tal-1β, Tal-2, MASH-1, AP-4, INSAP, HEN1</td>
</tr>
<tr>
<td>B</td>
<td>19</td>
<td>47% bHLH-bZip domains.</td>
<td>c-myc related factors (59%). Includes E-box type B TF. Related to cell proliferation.</td>
<td>Max1, Max2, AP-2αa, YB-1, Nmi, MAZ, SRRP1, Miz-1, Bin1, TRRAP, c-myc, dMax, Mxi1, MAd1, N-Myc, L-Myc(long form), Rox, GCN5, ADA2</td>
</tr>
<tr>
<td>C</td>
<td>30</td>
<td>36% rel homology región 40% bZip domains.</td>
<td>TF involved in NFκB pathway, AP1 complex and others</td>
<td>IRF-5, c-rel, NF-κB2 precursor, IκB-α, ATF-a, p65δ, NF-κB2(p49), NF-κB1 precursor, CRE-BPα, ATF3, HMGY, Fra-2, CEBPβ, ATF-2, RelA, c-fos, c-jun, p300, CBP, USF2, XBP-1, N-RK, GR-α, GR-β, Ref-1, CEBPA, CEBPB, ATF4, NF-AT1, NF-AT3</td>
</tr>
<tr>
<td>D</td>
<td>38</td>
<td>24% fork head domains.</td>
<td>E2F/pRB pathway, histone deacetylases (HDAC) [53,54]. PRB and p53 isoforms…</td>
<td>SRF, AR, STAT3, TFIIF-I, Net, Elk-1, SAP-1a, MhoX(K-2), Fl-1 α Egr-B, SAP-1b, BRF1, pRB, p130, DP-1, DP-2, E2F-1, E2F-2, E2F-3, p107, E2F-4, E2F-5, E2F-6, HDAC3, HDAC1, HDAC2, YAF2, ADA3, BRCa1, WT1, 53BP1, FLM-3, MTA1-L1, BAF47, p53, Y11, TGF, GATA-2, HDAC5</td>
</tr>
<tr>
<td>E</td>
<td>45</td>
<td>22% histone folding. Major part of specific interacting regions</td>
<td>Basal transcriptional machinery for promoters type I, II, III, PTF/SNAP complex and TBP related factors [39,51,52].</td>
<td>TFIIFα-β precursor(major), AREB6, TFIIF, TFIIF-α, TAFII131, TAFII-x1, 14-3-3c, CTF-1, TFIIF-β, TBP, TAFII170, TAFII130, TAFII170-β, Sp1, TAFII135, TAFII155, TAFII100, TAFII250, TAFII20, TAFII128, TAFII18, PUF1, ELF-1, CLIM2, POU2F2, TAFII110, TAFII54, NC2, PTFa, PTFβ, PTFβ, PC4, TFIIFγ, USF1, USF2b, CPA1, CEP1, CEP1C, RFXANK, CIITA, NF-YA, ZHX1, TFIIE-α, TFIIE-β</td>
</tr>
<tr>
<td>F</td>
<td>57</td>
<td>42% Zn finger domains.</td>
<td>It contains the 90% of the members of nuclear receptor superfamily (they are Zn fingers also) of the HTFN.</td>
<td>14-3-3 zeta, STAT1a, STAT1β, dCREB, ATF-1, TFF, NCO2, RBP-Jκ, TFIIF-Hp80, NCO1, RXR-α, TFIIF-Hp90, TFIIF-Hp62, TFIIF-CyclinH, TFIIF-MO15, TFIIF-MAT1, RAR-β, RARα1, RARγ1, POU2F1, TFIIF-Hp44, OCA-B, SRC-3, TRα1, RARγ1, RARβ1, VDR, SHP, PPAR-γ1, PPAR-β, RAR-α, RAR-β2, LXRα, FXR-α, CREB, STAT2, JunB, PPAR-γ2, FOXO3a, STAT6, SYT, TIF2, HNF-4, AhR, ER-α, COUP-TFI, BRG1, MOP3, ERR1, HIF-1α, Amt, SRC-1, HNF-4α2, EPAS1, HNF-4α, HNF-4α1</td>
</tr>
<tr>
<td>G</td>
<td>19</td>
<td>31% MAD domains.</td>
<td>SMAD family proteins and β-catenin and APC related factors.</td>
<td>ER-β, ZERF-P71, CtbP1, PGC-1, SKIP, Smad2, Smad3, Smad4, β-catenin, HOXB13, LEP-1, Evi-1, TCF-4E, TCF-4B, Pontin52, APC, Smad1, Smad6, Smad7</td>
</tr>
</tbody>
</table>

from the acquisition of a new level of complexity [25,26,28].
Regulation based on protein interactions makes it possible to find ‘transcriptional adaptors’ in the network. They are linking proteins with no other function. In fact, such transcriptional adaptors do appear in this web. This is the case of the previously described example, where pRB is unable to bind DNA alone [54] and interacts with E2F proteins in order to recruit histone deacetylases. Another example is NC2, a complex that acts as a general negative regulator of class II and III promoter gene expression, dimerizing via histone-fold structural motifs [51].

The evolution of HTFN could be also constrained by protein domain properties and their distribution along the proteins. In fact, using domain–domain coexistence in proteins as a way to establish links, it is possible to build a scale-free network in which very few domains are found related with many others [57]. In this context, it has been shown that some folds and superfamilies are extremely abundant, but most are rare [58]. Such heterogeneous distribution might suggest that only few domains have been suitable to undergo amplification.

Although tinkering based on domain reuse appears to be involved in shaping HTFN, part of the modularity cannot be explained by means of common structural features. Group D (basal transcriptional machinery) is a clear functional module lacking a homogeneous structural pattern. Proteins of this group form a bridge between RNA polymerases and cis elements in gene promoters. Initiation of transcription is an essential process pervading all other transcriptional-regulation events. Although histone-like folding in certain TAFII [52] is another example of reusing pre-existing solutions, it is remarkable that most of these complexes have been assembled by specific interacting regions. Such interaction could be given by a random process of optimization in which physical interaction was a solution (either directly or through molecular adaptors) to guarantee the colocalization of proteins that have to work together to perform a given function.

By contrast, bHLH and bZip domains have only the ability to bind DNA. Therefore, their essential role should be placed in their gene targets. Such systems emerged in order to improve regulation and may evolve without compromising essential functions, because they did not use the same type of connections of the basal machinery or other essential regulatory complexes. In this context, modularity should also be seen as a topological substrate in which the evolutionary trials would not compromise functionality of the whole network.

Conclusion

HTFNs share topological properties with other real networks. We have shown that the highly connected nodes are related to essential functions, and topological features retain functionality and phylogeny. However, the nature of the connections between these factors needs to be understood at the level of the protein domain. The global properties of the HTFN topology are partially due to specific interacting protein regions associated with the spatial and dynamical coordination of essential functions, together with tinkering processes based on protein domains reuse under initially slight selection pressures.

Future work must explore the dynamical context associated to the HTFN explored here at the topological level. A better picture of its robustness and how it relates to gene regulation will be obtained by considering networks dynamics. Also, given the special relevance of our elements to genome regulation, the dynamical effects on network stability after removing some particular components of the network can shed light into further evolutionary and biomedical questions.

Experimental procedures

Protein network data acquisition

HTFN was built using a specific transcription factor database (TRANSFAC 8.2 professional database) [31]. We restricted our search to Homo sapiens using the database OS (organism) field. Information concerning to physical interactions, derived from bibliographical sources, could be extracted from the database IN (interacting factor) field. TRANSFAC contains, as entries, not only single transcription factors but also some entries for well-described transcription complexes. To avoid identifying a protein complex as a single protein, which could cause false and redundant interactions, we eliminated those complexes by selecting only entries with SQ field (protein sequence), which is only present in single transcription factors.

Graph measures

Protein–protein interaction maps are complex networks. These networks are defined as sets of \( N \) nodes (the proteins, indicated as \( P_i, i = 1, \ldots, N \)) and \( L \) links among them. Two nodes will be linked only if they interact physically. The most basic parameters to describe such a network are as follows. (a) Degree \( (k_i) \) of a node defined as the number of links of such a node. The average degree \( \langle k \rangle \) will be simply defined as \( \langle k \rangle = 2L/N \). (b) Clustering coefficient \( (C_i) \); for a
node \( P_i \), it is the number of neighbouring of \( l_i \) links between nodes divided by the total number allowed by its degree, \( k_i \) \((k_i - 1)\). \( C_i \) tells us how interconnected the neighbours are. The clustering coefficient of the whole network is formally defined as:

\[
(C) = \frac{1}{N} \sum_{i=1}^{N} \frac{2l_i}{k_i(k_i - 1)}
\]

(c) The average path length \( L \) indicates the average number of nodes that separates each node from any other. If \( d_{\text{min}}(P_i, P_j) \) is the length of the shortest path connecting proteins \( P_i \) and \( P_j \), then \( L \) is defined as:

\[
L = \frac{2}{N(N - 1)} \sum_{i>j} d_{\text{min}}(P_i, P_j)
\]

(d) Betweenness centrality \( b_m \) for a node \( P_m \) is the number of short paths connecting pairs of nodes that contain the node \( P_m \) [59]. Specifically, for the \( m \)-th protein, it is the sum

\[
b_m = \sum_{i\neq j} \frac{\Gamma(i, m, j)}{\Gamma(i, j)}
\]

where \( \Gamma(i, m, j) \) is the number of the shortest paths between proteins \( P_i \) and \( P_j \), passing through \( P_m \), whereas \( \Gamma(i, j) \) is the total number of paths between those two proteins. The ratio \( \Gamma(i, m, j)/\Gamma(i, j) \) (assuming \( \Gamma(i, j) > 0 \)) weights how crucial the role of \( P_m \) is connecting \( P_i \) and \( P_j \). Average degree \( k \), clustering \( C \) and betweenness centrality \( b \) give us global information about the network. Using these parameters, it is possible to identify relevant properties of a complex web.

Real networks share the so-called ‘small-world’ behaviour (SW) [60,61], different to that shown by an Erdös-Rényi (ER) random network null model [62]. Typically, \( L_{\text{RW}} \sim L_{\text{ER}} \) and \( C_{\text{SW}} \gg C_{\text{ER}} \). Real networks also exhibit scale-free (SF) distributions of links, where the frequency of nodes with degree \( k \), \( f(k) \), decays according to a power-law distribution, i.e. \( f(k) = Ak^{-\gamma} \), with \( 2 < \gamma < 3 \) and \( A \) a constant. Here, we use the so-called cumulative distribution, defined as \( n(k) = \sum_{k=0}^{\infty} f(k) \). If \( f(k) \) follows a power law, the \( n(k) \) will also exhibit scale-freeness with an exponent \( \gamma_e = -\gamma + 1 \), because

\[
n(k) \approx \int_{k}^{\infty} Ak^{-\gamma}dk \sim k^{-\gamma+1}.
\]

For SF networks, most of the nodes are poorly connected and very few nodes (the so-called hubs) are highly connected. It has been shown that SF networks also exhibit power–law correlations for clustering and betweenness vs. degree [63,64]. Moreover, SF networks exhibit high homeostasis when nodes are removed at random. In contrast, if the most connected nodes are successively eliminated, the network becomes fragmented. However, a similar fragility is observed both if the nodes are removed at random or in order of increasing degree in random webs [61].

Compared with pure random ER and SF networks, biomolecular webs show the characteristic modular and hierarchical organization of biological systems [36], where clustering decays with the degree as \( C(k) \sim k^{-\gamma} \) [63]. This property is believed to confer additional stability, because failures in separate modules do not compromise the stability of the whole system. In this context, a related measure of network correlations associated to modular organization is provided by the coefficient \( r \) of assortative mixing [33]. This coefficient actually weights the correlation among the degrees of connected elements in a graph. It is defined as:

\[
r = \frac{L^{-1} \sum j_i k_i - (L^{-1} \sum j_i^2 + k_i^2)^{1/2}}{L^{-1} \sum j_i^2 (j_i + k_i)^2 - (L^{-1} \sum j_i^2)^{1/2}}
\]

where \( j_i \) and \( k_i \) are the degrees of the nodes located at the ends of the \( i \)-th link, with \( i = 1 \ldots L \). Defined in this way, it is such that \( -1 \leq r \leq 1 \), with negative values indicating disassortativeness and positive values indicating assortativeness. Most complex networks have been found to be disassortative, thus displaying hubs that are not directly connected among them.

### Graph distributions

Degree, betweenness and clustering distribution are shown in Fig. 2. We plot the distribution of these measures vs. degree on a log-log scale. Degree distribution (Fig. 2A) was measured using the cumulative frequency \( n(k) \) of nodes for each degree. In Fig. 2B,C we display the distribution of betweenness centrality and clustering against degree, respectively.

Both degree and betweenness centrality distributions are calculated by using the network dataset taking into account self-interactions. In any case, we obtained minor differences in the fitting of these distributions when self-interactions were not included. For the case of clustering, we show the network measures without interaction, because taking into account self-interaction leads to an overestimation of this measure. Power–law fitting was done using the cumulative degree distribution and the average value for betweenness centrality and clustering.

### Topological algorithms

#### Correlation profiles

The so-called correlation profile algorithm, defined in Maslov & Sneppen [34], compares the studied network with randomized versions of it with the same size and degree distribution. The so-called Z-score quantifies the difference between the studied network and an ensemble of randomized networks. \( Z \) is defined as \( Z(k_{0_0}, k_{1_1}) = (P(k_{0_0}, k_{1_1}) - P_{\text{RS}}(k_{0_0}, k_{1_1}))/\sigma_{\text{RS}}(k_{0_0}, k_{1_1}) \), where \( P(k_{0_0}, k_{1_1}) \) is the relative frequency of a pair of given link degrees, \( P_{\text{RS}}(k_{0_0}, k_{1_1}) \) is the same frequency but for a randomized network with the
same degree distribution than the studied one and, finally, 
\( \sigma_d(k_0, k_1) \) is the standard deviation of those ensemble randomized networks [34].

**Topological overlap matrix**

This algorithm gives information concerning network modularity. It arranges the nodes depending on the number of neighbours that they share. Afterwards, they are drawn in a bidimensional symmetric array where the strength of the relation between nodes is shown with a black to white gradient [36]. This algorithm also allows building a dendrogram that reflects the hierarchical relations between nodes. Other algorithms [65,66] have been tested providing similar results.

**Scaffold graph analysis**

This algorithm allows us to obtain a well-defined subgraph containing all the hub connections, and their interaction partners. One pair of connected proteins is conserved, in the so-called k-scaffold graph, if the degree of at least one protein of this pair is bigger than a predefined cut-off \( k_c \). By using this algorithm, both hubs and connectors among hubs are retained.

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**References**


